



## Teaching Guide

Identifying Data					2016/17
<b>Subject (*)</b>	Ampliación de matemáticas		<b>Code</b>	730496015	
<b>Study programme</b>	Mestrado Universitario en Enxeñaría Naval e Oceánica (plan 2012)				
Descriptors					
<b>Cycle</b>	<b>Period</b>	<b>Year</b>	<b>Type</b>	<b>Credits</b>	
Official Master's Degree	1st four-month period	First	Optativa	4.5	
<b>Language</b>	SpanishGalicianEnglish				
<b>Teaching method</b>	Face-to-face				
<b>Prerequisites</b>					
<b>Department</b>	Matemáticas				
<b>Coordinador</b>	Brozos Vázquez, Miguel	<b>E-mail</b>	miguel.brozos.vazquez@udc.es		
<b>Lecturers</b>	Brozos Vázquez, Miguel García Rodríguez, José Antonio	<b>E-mail</b>	miguel.brozos.vazquez@udc.es jose.garcia.rodriguez@udc.es		
<b>Web</b>	campusvirtual.udc.es/moodle				
<b>General description</b>	Nesta asignatura ampliaranse os conceptos matemáticos estudados nos graos de enxeñaría. Así, traballarase con curvas e superficies, comprendendo a súa xeometría e os elementos que a describen xunto coas ferramentas que usamos habitualmente para estudialas. Introducíranse conceptos básicos de cálculo tensorial e a súa aplicación na formulación e estudo de ecuacións en derivadas parciais que aparecen na física e na enxeñaría, con especial atención á mecánica de medios continuos.				

## Study programme competences / results

Code	Study programme competences / results
B1	Posuír e comprender coñecementos que acheguen unha base ou oportunidade de ser orixinais no desenvolvemento e/ou aplicación de ideas, a miúdo nun contexto de investigación
B2	Que os estudantes saiban aplicar os coñecementos adquiridos e a súa capacidade de resolución de problemas en ámbitos novos ou pouco coñecidos dentro de contextos máis amplos (ou multidisciplinares) relacionados coa súa área de estudo
B4	Que os estudantes saiban comunicar as súas conclusións e os coñecementos e razóns últimas que as sustentan a públicos especializados e non especializados dun modo claro e sen ambigüidades.
B5	Que os estudantes posúan as habilidades de aprendizaxe que lles permitan continuar estudando dun modo que haberá de ser en boa medida autodirixido ou autónomo.
B6	Ser capaz de realizar unha análise crítica, avaliación e síntese de ideas novas e complexas.

## Learning outcomes

Learning outcomes	Study programme competences / results
Ability to work with curves and surfaces and study their geometric properties: curvature, geodesics, ...	BC1 BC2 BC4 BC5 BC6
Application of tensor calculus to the formulation of partial differential equations from Physics.	BC1 BC2 BC5
Knowledge of elementary tensor calculus	BC1 BC2
Capability to face typical problems in the context of naval engineering using basic differential geometry of curves and surfaces.	BC1 BC5 BC6



Contents	
Topic	Sub-topic
Curves	Parametrized curves. Regular curves. Arc length. Curvature. Torsion. Frenet trihedron. Famous curves.
Surfaces	Parametrized surfaces. Regular surfaces. Tangent plane. First fundamental form. Surface area. Tensor fields. The metric tensor. Second fundamental form. Christoffel symbols. Gauss curvature and mean curvature. Ruled surfaces and minimal surfaces.  Appendix 1: Einstein notation. Appendix 2: bilinear forms and quadratic forms.
Mathematics of continuum mechanics. Conservations laws	<ul style="list-style-type: none"> <li>- Continuum cinematics</li> <li>- Gradient of strain tensor. Green-Saint Venant Strain tensor</li> <li>- Transformation of areas and volumes</li> <li>- Reynolds theorem of transport.</li> <li>- Mass conservation law.</li> <li>- Law of conservation of momentum</li> <li>- Thermodynamics. Law of conservation of energy</li> <li>- Control volumens and conservation laws</li> </ul>
Partial differential equations	<ul style="list-style-type: none"> <li>- Partial differential equations. Boundary conditions.</li> <li>- Constitutive laws</li> <li>- Fluid mechanics. Derivation of some important equations in fluid mechanics.</li> </ul> Equations for incompressible fluids. <ul style="list-style-type: none"> <li>- Elastic solids. Cauchy Theorem. Stress and strain tensors. Principal components.</li> <li>Eigenvalues and eigenvectors. Partial differential equations para for elastic solids.</li> </ul>

Planning				
Methodologies / tests	Competencies / Results	Teaching hours (in-person & virtual)	Student?s personal work hours	Total hours
Guest lecture / keynote speech	B1 B2 B5 B6	24	36	60
Problem solving	B1 B2 B4 B5 B6	12	12	24
Supervised projects	B2 B4 B5 B6	0	24	24
Objective test	B1 B2 B4 B5 B6	3.5	0	3.5
Personalized attention		1	0	1

(\* )The information in the planning table is for guidance only and does not take into account the heterogeneity of the students.

Methodologies	
Methodologies	Description
Guest lecture / keynote speech	Oral presentation complemented with the use of audiovisual media and the introduction of some questions to the students, in order to transmit knowledge and provide learning
Problem solving	Technique of group work which purpose is the in-depth study of a subject. It involves discussion, participaction, edocuments elaboration and the conclusion reached by all the components of the seminar.



Supervised projects	Methodology designed to promote autonomous learning of the students, always under the teacher's guide. It is a technique based on the assumption by the students of the responsibility of their learning. This learning technique is based in two basic elements: the autonomous learning and the continuous monitoring of this learning by the teachers.
Objective test	Written test to assess the obtained competencies. It is an instrument of measure, rigorously developed, that allows to evaluate knowledges, capacities, skills, performances, aptitudes, attitudes, etc.

**Personalized attention**

Methodologies	Description
Supervised projects	Along the course several works will be proposed to the students, and that will allow them, in case of obtaining a positive evaluation, to pass the subject.

**Assessment**

Methodologies	Competencies / Results	Description	Qualification
Objective test	B1 B2 B4 B5 B6	At the end of the course, these students that have not done the proposed works or that want to obtain a better qualification, will do a written exam in the data fixed by the school.	50
Supervised projects	B2 B4 B5 B6	Students who wish to, can choose a topic from among those proposed by the teachers of the subject. They will do a work on this subject to deepen their concepts and techniques, and that they will have to expose later. This work will be qualified and will allow to pass the subject.	50

**Assessment comments**

The works will be corrected and attending to this corrections students will be qualified. If a student does not present the proposed work or if he/she wants to obtain a better qualifications, he/she will be able to give up the obtained qualification and do the final exam.

**Sources of information**

<b>Basic</b>	<ul style="list-style-type: none"> <li>- Alexandre J. Chorin, Jerrold E. Marsden. (2000). A Mathematical Introduction to Fluid Mechanics. Texts in Applied Mathematic, Springer</li> <li>- Rutherford Aris (1962). Vectors, tensors, and the basic equations of fluid mechanics.. Prentice-Hall</li> <li>- Manfredo P. do Carmo (1995). Geometría diferencial de curvas y superficies. Alianza Universidad Textos</li> <li>- José A. Pastor González, M<sup>a</sup> Ángeles Fernández Cifre (2010). Un curso de geometría diferencial. Consejo Superior de Investigaciones Científicas</li> <li>- M. Gurtin (1981). An introduction to continuum mechanics. Academic Press</li> <li>- M. Gurtin, Eliot Fried, Lallit Anand (2010). The mechanics and thermodynamics of continua. Cambridge</li> </ul>
<b>Complementary</b>	

**Recommendations**

**Subjects that it is recommended to have taken before**

**Subjects that are recommended to be taken simultaneously**

**Subjects that continue the syllabus**

**Other comments**



(\*)The teaching guide is the document in which the URV publishes the information about all its courses. It is a public document and cannot be modified. Only in exceptional cases can it be revised by the competent agent or duly revised so that it is in line with current legislation.