



Teaching Guide				
Identifying Data				2020/21
Subject (*)	Mathematics I	Code	631G01101	
Study programme	Grao en Náutica e Transporte Marítimo			
Descriptors				
Cycle	Period	Year	Type	Credits
Graduate	1st four-month period	First	Basic training	6
Language	SpanishGalician			
Teaching method	Hybrid			
Prerequisites				
Department	Matemáticas			
Coordinador	Rodríguez Aros, Angel Daniel	E-mail	angel.aros@udc.es	
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Web	www.nauticaymaquinas.es/			
General description	This course is devoted to the study of the basic results and applications of classical subjects in mathematics: Linear Algebra, Euclidean Geometry, Functional Analysis and Complex Variable. The student will learn to use these specific mathematical tools, but also they will improve their skills in developing new methods and acquiring new technologies, to consult bibliographic references and online resources, to elaborate a memory in a rigorous and systematic manner, to give lectures to others and collaborate with other colleagues, etc. In general they will develop a sense of scientific and rational thinking, capable to adapt to unexpected situations which may arise in their future practice as an engineer.			
Contingency plan	<ol style="list-style-type: none"> <li>1. Modifications to the contents</li> <li>2. Methodologies <ul style="list-style-type: none"> <li>*Teaching methodologies that are maintained</li> <li>*Teaching methodologies that are modified</li> </ul> </li> <li>3. Mechanisms for personalized attention to students</li> <li>4. Modifications in the evaluation <ul style="list-style-type: none"> <li>*Evaluation observations:</li> </ul> </li> <li>5. Modifications to the bibliography or webgraphy</li> </ol>			

Study programme competences / results	
Code	Study programme competences / results
A2	Interpretar e representar correctamente o espazo tridimensional, coñecendo os obxectivos e o emprego de representación gráfica.
A8	Modelizar situacións e resolver problemas con técnicas ou ferramentas físico-matemáticas.
A9	Avaliación cualitativa e cuantitativa de datos e resultados, así como representación e interpretación matemática de resultados obtidos experimentalmente.
B1	Aprender a aprender.
B2	Resolver problemas de xeito efectivo.
B3	Aplicar un pensamento crítico, lóxico e creativo.
B4	Comunicarse de xeito efectivo nun ámbito de traballo.
B5	Traballar de forma autónoma con iniciativa.
B6	Traballar de forma colaboradora.



B7	Comportarse con ética e responsabilidade social como cidadán e como profesional.
B8	Aprender en ámbitos de teleformación.
B9	Capacidade para interpretar, seleccionar e valorar conceptos adquiridos noutras disciplinas do ámbito marítimo, mediante fundamentos físico-matemáticos.
B10	Versatilidade.
B11	Capacidade de adaptación a novas situacións.
B12	Uso das novas tecnoloxías TIC, e de Internet como medio de comunicación e como fonte de información.
B13	Comunicar por escrito e oralmente os coñecementos procedentes da linguaxe científica.
B14	Capacidade de análise e síntese.
B15	Capacidade para adquirir e aplicar coñecementos.
B16	Organizar, planificar e resolver problemas.
B17	Expresarse correctamente, tanto de forma oral coma escrita, nas linguas oficiais da comunidade autónoma
B19	Utilizar as ferramentas básicas das tecnoloxías da información e as comunicacións (TIC) necesarias para o exercicio da súa profesión e para a aprendizaxe ao longo da súa vida.
B22	Valorar criticamente o coñecemento, a tecnoloxía e a información dispoñible para resolver os problemas cos que deben enfrontarse.
B23	Asumir como profesional e cidadán a importancia da aprendizaxe ao longo da vida.
B24	Valorar a importancia que ten a investigación, a innovación e o desenvolvemento tecnolóxico no avance socioeconómico e cultural da sociedade.
C10	Que os estudantes saiban aplicar os coñecementos adquiridos e a súa capacidade de resolución de problemas en contornas novas ou pouco coñecidas dentro de contextos máis amplas (ou multidisciplinares) relacionados coa súa área de estudo

Learning outcomes			
Learning outcomes	Study programme competences / results		
Do listado de competencias da titulación	A2		
	A8		
	A9		
Do listado de competencias da titulación		B1	
		B2	
		B3	
		B4	
		B5	
		B6	
		B7	
		B8	
		B9	
		B10	
		B11	
		B12	
		B13	
		B14	
		B15	
		B16	
		B17	
		B19	
		B22	
		B23	
		B24	
Do listado de competencias da titulación			C10



Contents	
Topic	Sub-topic
Lesson 1.- Espazos Vectoriais	1.1.- Vector space. Definition. Examples and Properties 1.2.- Vector subspace. 1.3.- System of Generators of a Subspace 1.4.- Linear Independence 1.5.- Basis of a Vector Space. Finite Dimensional Spaces. 1.6.- Change of Basis in a Vector Space 1.7.- Union and Intersection of Subspaces 1.8.- Sum of Subspaces. Direct sum. Supplementary Subspaces. 1.9.- Product of Vectorial Spaces
Lesson 2.- Linear Functions. Matrices.	2.1.- Linear Function: Definition, Examples, Properties and Types of Linear Functions. 2.2.- Kernel and Image of a Linear Function. 2.3.- Existence and obtention of an Associated Matrix to a Linear Function. 2.4.- Addition of Linear Functions. Product by a Scalar. Associated Matrices. 2.5.- Vector Spaces of Matrices 2.6.- Composition of Linear Functions. Associated Matrix. 2.7.- Product of Matrices. Ring of Square Matrices 2.8.- Some Particular Types of Matrices 2.9.- Transpose Matrix. Symmetric, Antisymmetric and Orthogonal Matrices. 2.10.- Matrices of Complex Elements.
Lesson 3.- Determinants.	3.0.- Permutations. Class of a Permutation. 3.1.- Determinant of a Square Matrix. Sarrus Rule. 3.2.- Properties of Determinants. 3.3.- Methods for Calculation of Determinants. Cofactor Matrix. 3.4.- Product of Determinants. 3.5.- Some Particular Examples of Determinants. 3.6.- Reverse Matrix. 3.7.- Rank of a Matrix. 3.8.- Rank of a System of Vectors 3.9.- Expression of the Change of Base of a Vectorial Space in shape Matrix
Lesson 4.- Systems of Linear Equations.	4.1.- Definitions. Classification. Matrix notation. 4.2.- Equivalent systems. 4.3.- System of Cramer. Rule of Cramer 4.4.- General System of Linear Equations. Theorem of Rouché-Frobenius 4.5.- Homogeneous Systems. 4.6.- Methods of Resolution by Reduction. Gauss' Method.
Lesson 5.- Matrix Diagonalization.	5.1.- Eigenvectors and Eigenvalues. Properties. 5.2.- Characteristic polynomial. Properties. 5.3.- Diagonalizable Matrices. Diagonalization. 5.4.- Diagonalization Of Symmetric Matrices.
Lesson 6.- Affine Space E3. Problems of Incidence and Parallelism.	6.1.- Affine Space Associated to a Vector Space. System of Reference. Coordinates. 6.2.- Equations of Straight Lines. 6.3.- Relative positions of Straight Lines. 6.4.- Equations of a Plane. 6.5.- Relative positions of Planes. Bundles of Planes. 6.6.- Relative positions of Straight Lines and Planes.



Lesson 7.- Euclidean Vector Spaces. Scalar product, Vector product. Mixed Product.	7.1.- Scalar product 7.2.- Determination of a Scalar Product. Gram Matrix. 7.3.- Euclidean Vector Space. Definition. 7.4.- Norm of a Vector. Relevant Equalities and Inequalities. 7.5.- Angle of two Vectors. Orthogonality. 7.6.- Orthonormal Basis. Expression of the Scalar Product in an Orthonormal Basis. 7.7.- Euclidean Space $E^3$ . 7.8.- Orientation in $E^3$ . 7.9.- Vector product in $R^3$ . Properties. Analytical expression. 7.10.- Mixed product. Analytical expression. Geometrical interpretation. 7.11.- Combined Products.
Lesson 8.- Metric Problems in Euclidean Spaces.	8.1.- Normal equation of a Plane. 8.2.- Angles between Linear Manifolds in $R^3$ : Angle of Two Planes, Angle of Two Straight Lines, Angle of Straight Line and Plane. 8.3.- Distance between Linear Manifolds in $R^3$ : Distance of a Point to a Plane, Distance of a Point to a Straight Line. Distance between two Planes, Distance between Straight Line and Plane. Distance between two Straight Lines. Common Perpendicular to two Straight Lines. 8.4.- Cylindrical coordinates and Spherical coordinates in $R^3$ .
Lesson 9.-Real valued functions of a Real Variable. Continuity.	9.1.- Basic definitions. 9.2.- Functional limits. 9.3.- Continuity. Types of Discontinuity. 9.4.- Properties and Theorems on Continuous Functions.
Lesson 10.- Differentiability and Applications of the Derivatives.	10.1.- Derivative and Differential of a Function in a Point. Geometrical meaning. 10.2.- Properties and Calculation of Derivatives. 10.3.- Derivative function. Successive derivatives. 10.4.- Applications of the Derivatives to the Local Study of a Function: Growth and Decreasing. Maxima and Minima. Concavity and Convexity. Inflection points. 10.5.- Theorems of Rolle and Mean Value Theorem. 10.6.- Rules of L'Hôpital
Lesson 11.- Theorem of Taylor. Applications.	11.1.- Expression of a Polynomial by means of his Derivatives in a Point. 11.2.- Polynomial and Theorem of Taylor. Formulae of Taylor and Mac Laurin. 11.3.- Expression of Lagrange for the Residual. Bounds for the residual. 11.4.- Applications to the Local Study of a Function: Monotonicity. Extremal values. Concavity and Convexity. Inflection points.
Lesson 12.- Graphic representation of Real Valued Functions.	12.1.- Domain and Continuity 12.2.- Symmetries 12.3.- Periodicity. 12.4.- Intersection with the coordinates axis. 12.5.- Use of successive derivatives and applications: Monotonicity. Extremal values. Concavity and Convexity. Inflection points. 12.6.- Asymptotes and Parabolic Branches



Lesson 13.- Sequences and Series.	<p>13.1.- General definitions. Types of Sequences.</p> <p>13.2.- Practical calculation of Limits</p> <p>13.3.- General definitions. Main Types of Numerical Series.</p> <p>13.4.- Properties of the Numerical Series. Criteria of Convergence for Series of Positive Terms.</p> <p>13.5.- Series of Positive and Negative Terms. Alternated Series.</p>
Lesson 14.- Functional Sequences and Series. Series of powers.	<p>14.1.- General definitions.</p> <p>14.2.- Series of Powers. Convergence.</p> <p>14.3.- Series expansions.</p> <p>14.4.- Series of Taylor and Mac Laurin.</p> <p>14.5.- Binomial Series.</p> <p>14.6.- Method of the Undetermined Coefficients.</p>
Lesson 15.- Indefinite integration of Functions of a Real Variable	<p>15.1.- General definitions. Table of Primitives.</p> <p>15.2.- Immediate integration</p> <p>15.3.- Integration by Parts</p> <p>15.4.- Integration of Rational Functions</p> <p>15.5.- Integration by Replacement or Change of Variable</p>
Lesson 16.- Definite Integration. Applications.	<p>16.1.- General definitions</p> <p>16.2.- Properties</p> <p>16.3.- Mean Value Theorem. Barrow's Rule.</p> <p>16.4.- Evaluation of Definite Integrals.</p> <p>16.5.- Improper Integral.</p> <p>16.6.- Applications of the Definite Integral</p>
Lesson 17.- Complex Numbers	<p>17.1.- General definitions</p> <p>17.2.- Fundamental operations</p> <p>17.3.- Powers and Roots</p> <p>17.4.- Exponential form of a Complex</p> <p>17.5.- Logarithms And Complex Powers.</p>
The development and overcoming of these contents, together with those corresponding to other subjects that include the acquisition of specific competencies of the degree, guarantees the knowledge, comprehension and sufficiency of the competencies contained in Table AII / 2, of the STCW Convention, related to the level of management of chief mates of the Merchant Navy, on ships without gross tonnage limitation and Master up to a maximum of 500 GT.	<p>Table A-II / 2 of the STCW Convention.</p> <p>Mandatory minimum requirements for certification of masters and chief mates on chief on ships of 500 gross tonnage or more.</p>

### Planning

Methodologies / tests	Competencies / Results	Teaching hours (in-person & virtual)	Student?s personal work hours	Total hours
Document analysis	<p>A2 A8 B1 B2 B3 B4</p> <p>B5 B6 B8 B9 B10 B11</p> <p>B12 B13 B14 B15</p> <p>B16 B17 B19 B22 C3</p> <p>C8</p>	0	2	2



Collaborative learning	A9 B1 B3 B4 B6 B7 B8 B9 B10 B11 B12 B13 B17 B23 B24 C1 C3 C6 C7 C8 C10	9	9	18
Online discussion	A8 A9 B2 B3 B4 B5 B6 B8 B9 B10 B11 B12 B13 B14 B15 B17 B19 B22 B24 C3 C6 C8 C10	0	6	6
Diagramming	A8 A9 B1 B2 B4 B5 B8 B9 B11 B12 B13 B14 B16 C1 C3	2	4	6
Directed discussion	A2 A8 A9 B1 B2 B3 B4 B5 B6 B7 B8 B9 B10 B11 B12 B13 B14 B15 B16 B17 B19 B22 B23 B24 C1 C3 C6 C7 C8 C10	2	0	2
Supervised projects	A2 A8 A9 B1 B2 B3 B4 B5 B6 B8 B9 B12 B13 B14 B15 B16 B17 B19 B22 B23 B24 C1 C3 C6 C7 C10	4	20	24
Guest lecture / keynote speech	A2 A8 B1 B2 B3 B4 B15 B22 C1 C6 C8 C10	24	24	48
Objective test	A2 A8 A9 B2 B4 B5 B11 B12 B13 B14 B16 B17 B19 B22 B23 C1 C3 C10	4	0	4
Problem solving	A2 A8 A9 B2 B5 B6 B10 B11 B12 B13 B15 B16 B17 B19 C1 C3 C6 C10	6	24	30
Introductory activities	B1 B3 B4 B6 B7 B8 B14 B15 B23 C10	3	3	6
Personalized attention		4	0	4

(\*)The information in the planning table is for guidance only and does not take into account the heterogeneity of the students.

Methodologies	
Methodologies	Description
Document analysis	Seleccionar libros e páxinas web a utilizar
Collaborative learning	Traballo en grupo con exposición dos resultados no seu caso
Online discussion	Plantexar e resolver dudas en Moodle
Diagramming	Rematar cada tema con un esquema dos conceptos básicos aprendidos.
Directed discussion	Discusión na aula do plantexado previamente en Moodle ou en clase.
Supervised projects	Traballos propostos individuais e grupais
Guest lecture / keynote speech	Exposición na aula dos conceptos fundamentais. Para os estudantes que non poidan seguir as clases de modo presencial, éstas retransmitíranse e graváranse mediante a plataforma MS Teams.



Objective test	Proba de coñecementos.
Problem solving	En cada tema, se propondrán exercicios para resolver.
Introductory activities	Tema 0: Conceptos básicos que se deben recordar

### Personalized attention

Methodologies	Description
Problem solving Supervised projects	The students are encouraged to attend in small groups or individually to the professors' office to solve questions that may arise, thus obtaining a more specific guidance, according to their specific difficulties.

### Assessment

Methodologies	Competencies / Results	Description	Qualification
Problem solving	A2 A8 A9 B2 B5 B6 B10 B11 B12 B13 B15 B16 B17 B19 C1 C3 C6 C10	Resolver problemas.	20
Objective test	A2 A8 A9 B2 B4 B5 B11 B12 B13 B14 B16 B17 B19 B22 B23 C1 C3 C10	Proba para amosar os coñecementos teóricos e prácticos adquiridos.	50
Collaborative learning	A9 B1 B3 B4 B6 B7 B8 B9 B10 B11 B12 B13 B17 B23 B24 C1 C3 C6 C7 C8 C10	Participación en traballos grupais.	5
Supervised projects	A2 A8 A9 B1 B2 B3 B4 B5 B6 B8 B9 B12 B13 B14 B15 B16 B17 B19 B22 B23 B24 C1 C3 C6 C7 C10	Traballos propostos.	20
Directed discussion	A2 A8 A9 B1 B2 B3 B4 B5 B6 B7 B8 B9 B10 B11 B12 B13 B14 B15 B16 B17 B19 B22 B23 B24 C1 C3 C6 C7 C8 C10	Participación nos debates na aula.	5

### Assessment comments



The course is divided into two parts: Part 1 (lessons 1-8) and part 2 (lessons 9-17). To pass it, it will be necessary to reach in each part a minimum of 3,5 points and afterwards obtain an average of, at least, 5 points.

In the unlikely case of reaching an arithmetic average of 5 but not having, at least, 3,5 points in each one of the parts, the result of the evaluation will be of fail and the final qualification will be calculated with a suitable geometric average.

The students that do not participate in the EHEA will be evaluated through a written test that will constitute 100% of the evaluation. For those who participate in the EHEA, the written test will constitute 70% of the final marks. In order to add the qualification of the continuous assessment to the qualification of the written test, the latter must be at least 2,4 points (approximately 35% of 7) for each part, otherwise the final mark will only account for the written test.

Those students with recognition of part-time dedication and academic exemption of attendance, as established by the norm that regulates the regime of dedication to the study of undergraduate students in the UDC (Arts 2.3, 3.b, 4.3 e 7.5 ) (04/05/2017), and want to stay on the path of the EHEA and benefit from continuous assessment, must attend at least 50% of the course, exempting them from attending the theoretical classes, if they can not attend them. In case of not being able to attend the practical tests, they should attend tutorials at the professor office, where they will perform equivalent tests.

### Sources of information

<b>Basic</b>	<ul style="list-style-type: none"> <li>- Granero, F (). ALGEBRA Y GEOMETRÍA ANALÍTICA . Mac Graw-Hill</li> <li>- Fernández Viña, J.A (). ANÁLISIS MATEMÁTICO I . Tecnos</li> <li>- Granero, F. (). CÁLCULO . Mac Graw-Hill</li> <li>- García , A.y otros. (). CÁLCULO I (Teoría y Problemas) . Librería I.C.A.I</li> <li>- Granero, F. (). EJERCICIOS Y PROBLEMAS DE CÁLCULO (I y II) . Tébar Flores</li> <li>- Villa, A. de la (). PROBLEMAS DE ALGEBRA LINEAL. GLAGSA</li> <li>- D.G. Zill, W.S. Wright, J. Ibarra (). Matemáticas 1. Cálculo Diferencial. McGraw Hill</li> <li>- D.G. Zill, W.S. Wright, J. Ibarra (). Matemáticas 2. Cálculo Integral. McGraw Hill</li> <li>- S. Grossman, J. Ibarra (). Matemáticas 4. Álgebra Lineal. McGraw Hill</li> <li>- Á.M. Ramos del Olmo, J.M. Rey Cabezas (2017). Matemáticas básicas para el acceso a la universidad. Pirámide</li> </ul>
<b>Complementary</b>	

### Recommendations

#### Subjects that it is recommended to have taken before

#### Subjects that are recommended to be taken simultaneously

Physics/631G01103

#### Subjects that continue the syllabus

Mathematics II/631G01106

#### Other comments

Attend the optional introductory course which is given the first week.

(\*The teaching guide is the document in which the URV publishes the information about all its courses. It is a public document and cannot be modified. Only in exceptional cases can it be revised by the competent agent or duly revised so that it is in line with current legislation.